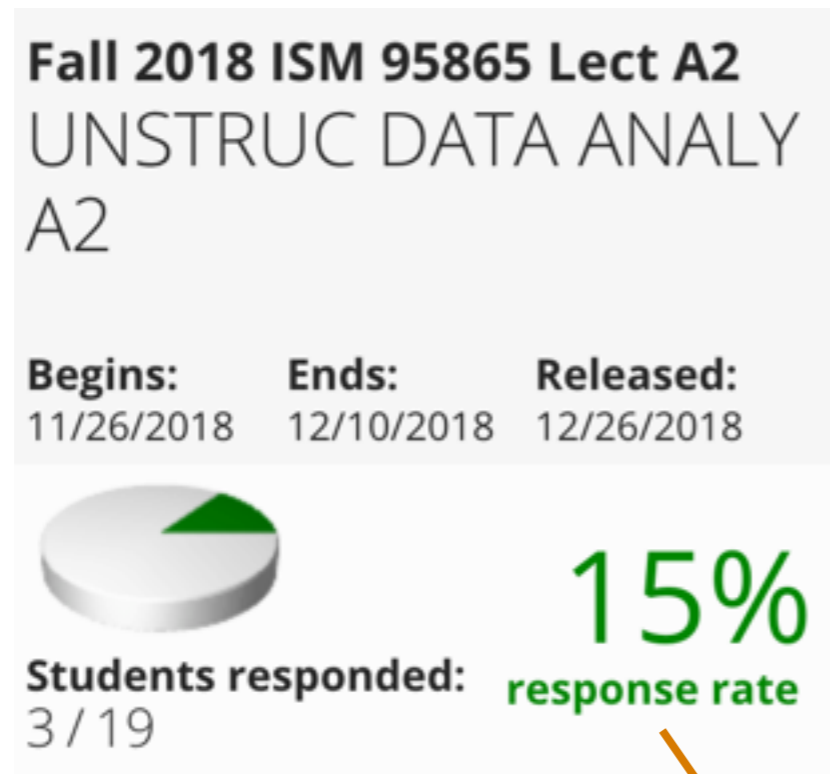


**95-865 Pittsburgh Lecture 10:
Image Analysis With
Convolutional Neural Nets**

George Chen

Faculty Course Evaluations

Please provide valuable feedback/vent your frustration

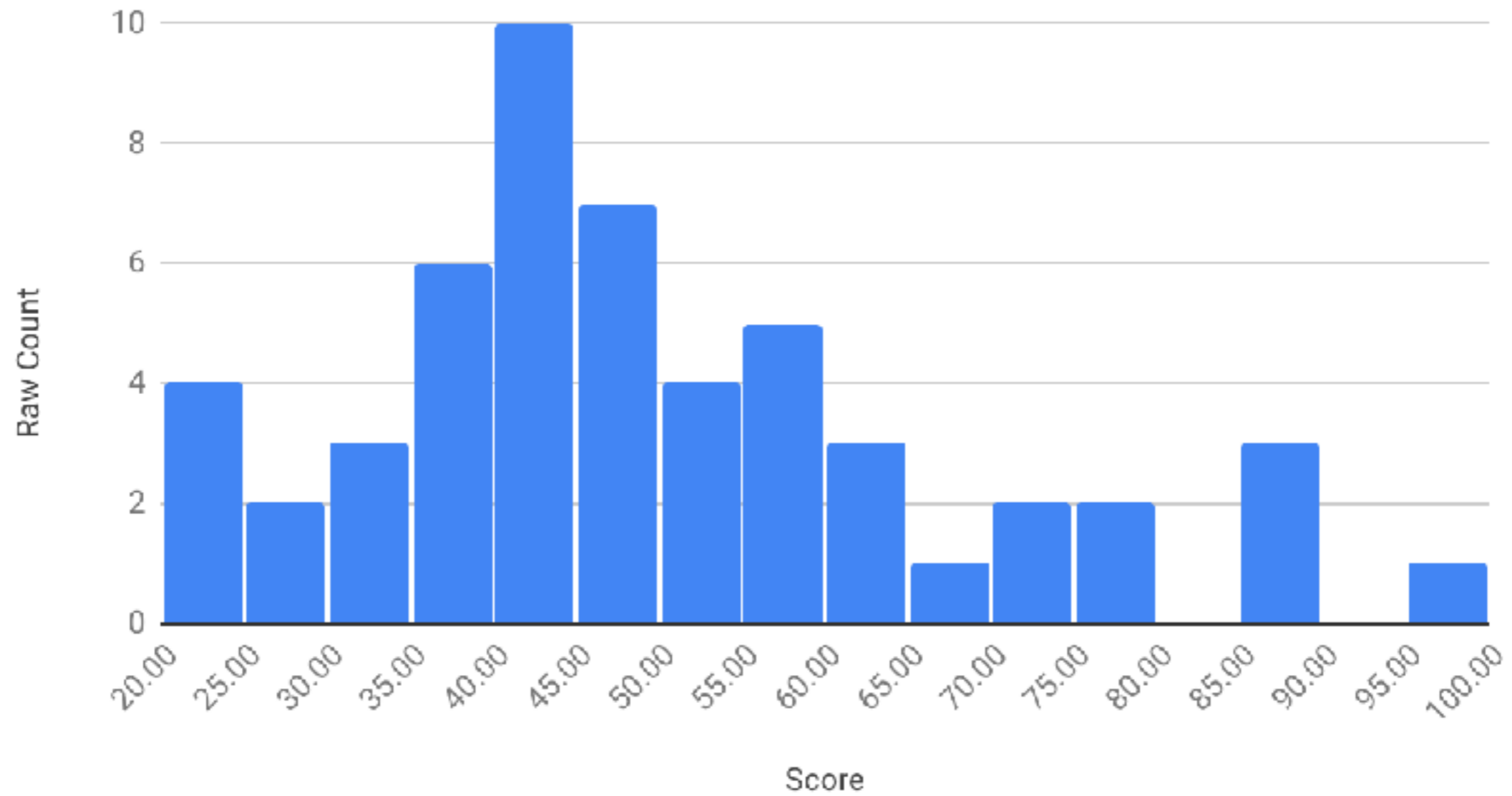


If you're not sure what to write about:

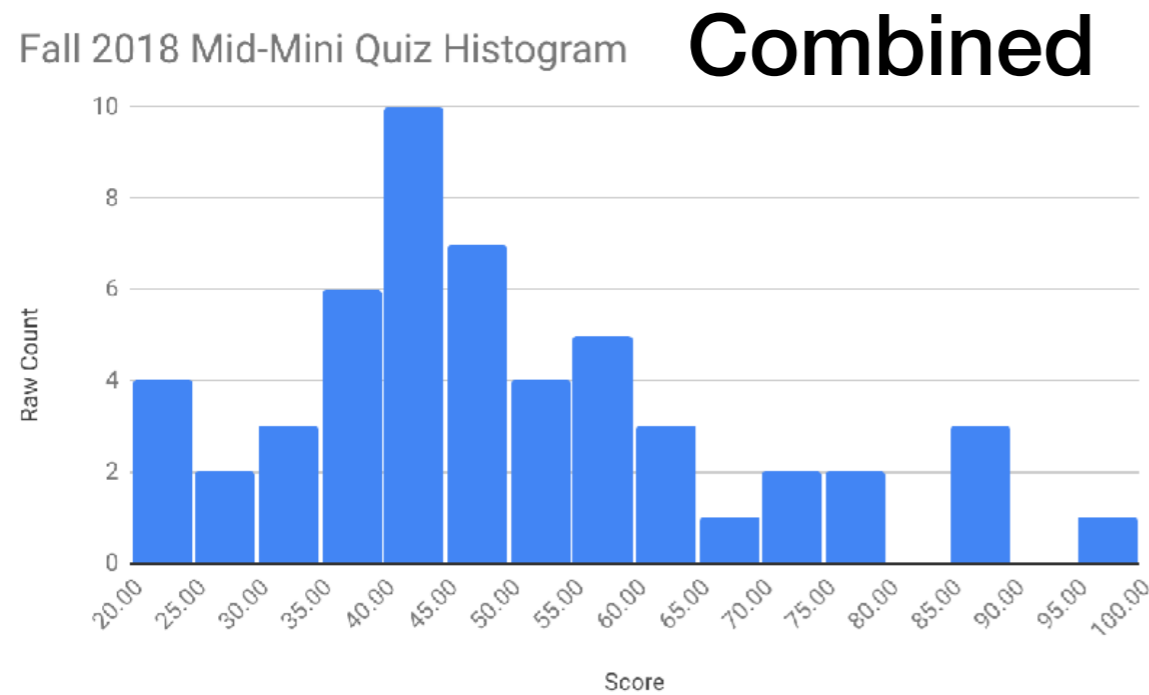
- what additional Python prep *prior* to taking the course would have been helpful?
- what Python review *during* the course would have been helpful?
- most/least favorite parts of the course?

Quiz Results

Fall 2018 Mid-Mini Quiz Histogram

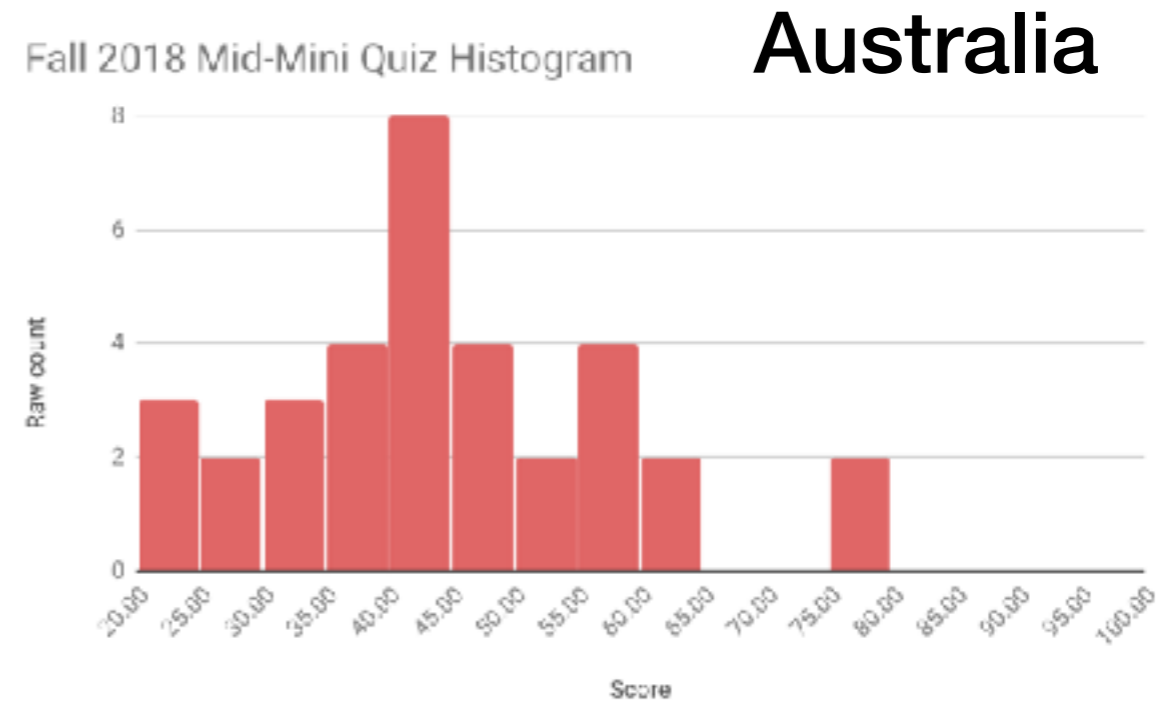


Quiz Results

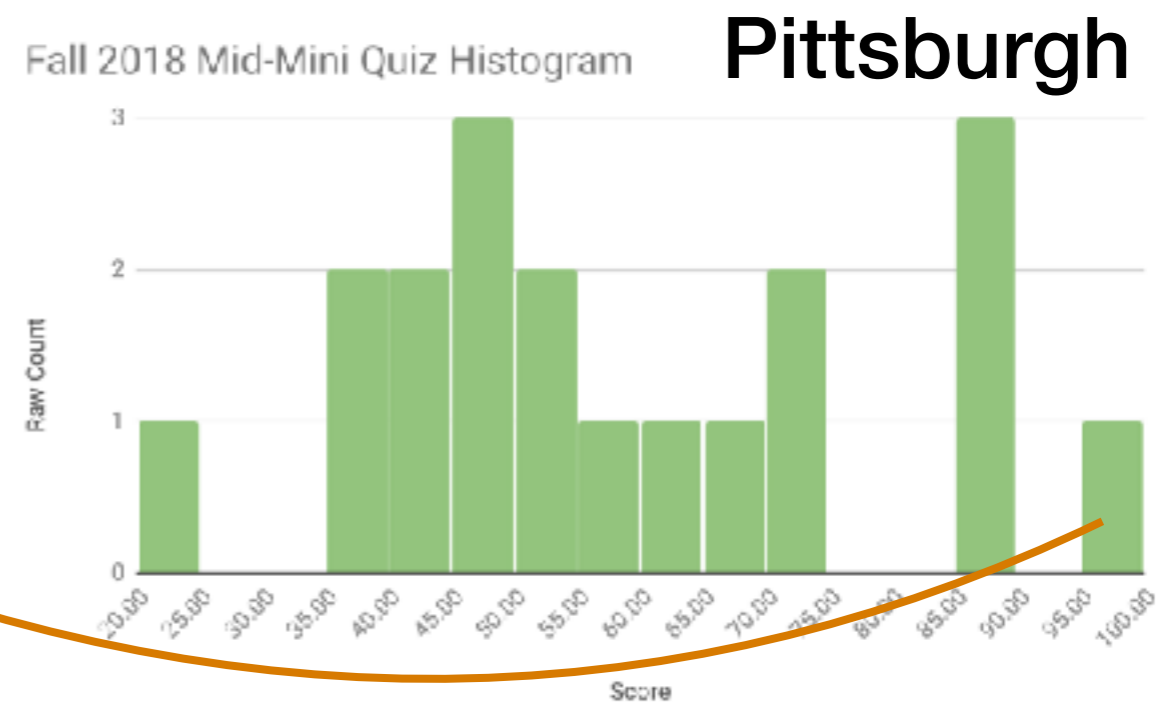


Mean: 49.3, std dev: 17.8

Max score achieved: 98



Mean: 44.1, std dev: 13.6



Mean: 58.6, std dev: 20.5

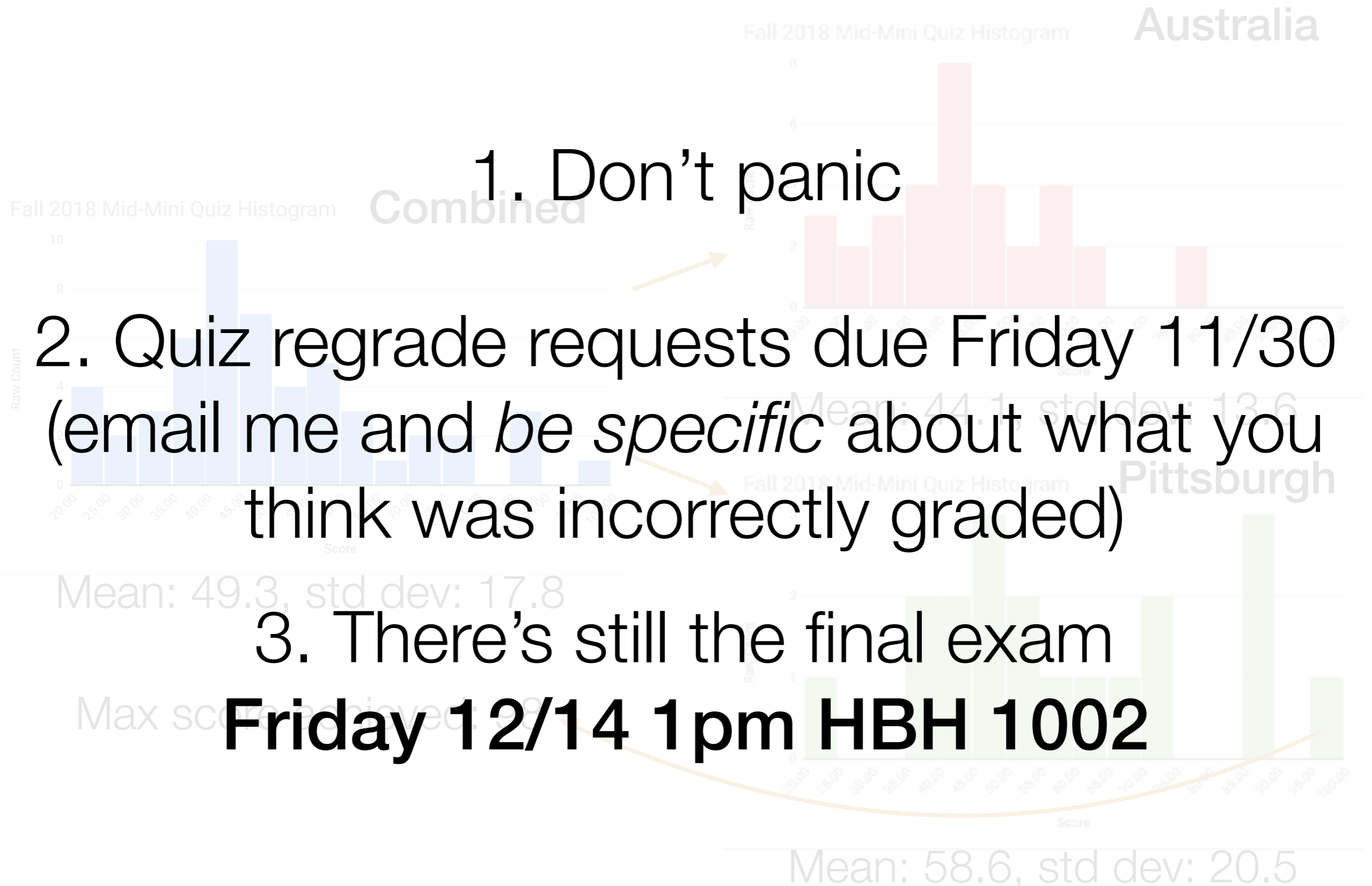
Quiz Results

1. Don't panic

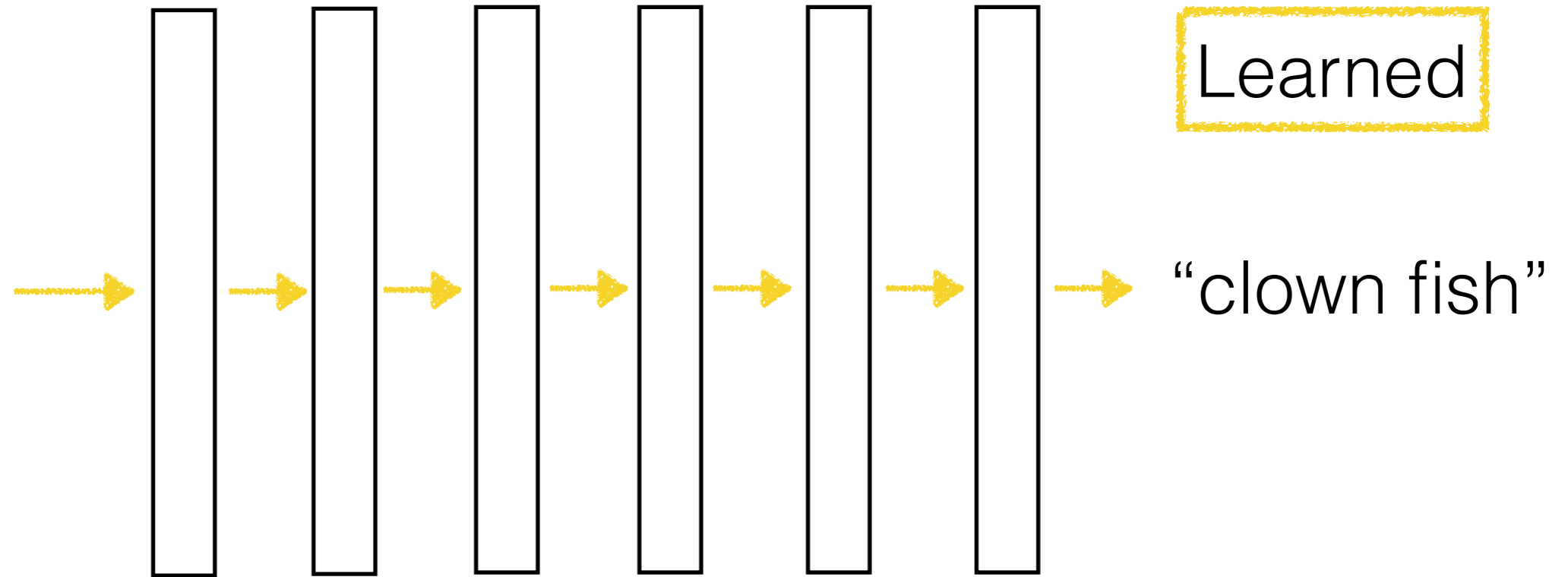
2. Quiz regrade requests due Friday 11/30
(email me and *be specific* about what you think was incorrectly graded)

3. There's still the final exam

Friday 12/14 1pm HBH 1002



Deep Learning



- Inspired by biological neural nets *but otherwise not the same at all* (biological neural nets do *not* work like deep nets)
- Learns a layered representation
 - Tries to get rid of manual feature engineering
 - Need to design constraints for what features are learned to account for structure in data (e.g., images, text, ...)

Learning a neural net amounts to curve fitting

We're just estimating a function

Neural Net as Function Approximation

Given `input`, learn a `computer program` that computes `output`

this is a **function**

Single-layer neural net example:

```
def f(input):
```

```
    output = softmax(np.dot(W, input) + b)
```

```
    return output
```

the only things that we are learning
(we fix their dimensions in advance)

We are fixing what the function `f` looks like in code
and are only adjusting `W` and `b`!!!

Neural Net as Function Approximation

Given `input`, learn a computer program that computes `output`

Single-layer neural net example:

```
output = softmax(np.dot(W, input) + b)
```

Two-layer neural net example:

```
layer1_output = relu(np.dot(W1, input) + b1)
```

```
output = softmax(np.dot(W2, layer1_output) + b2)
```

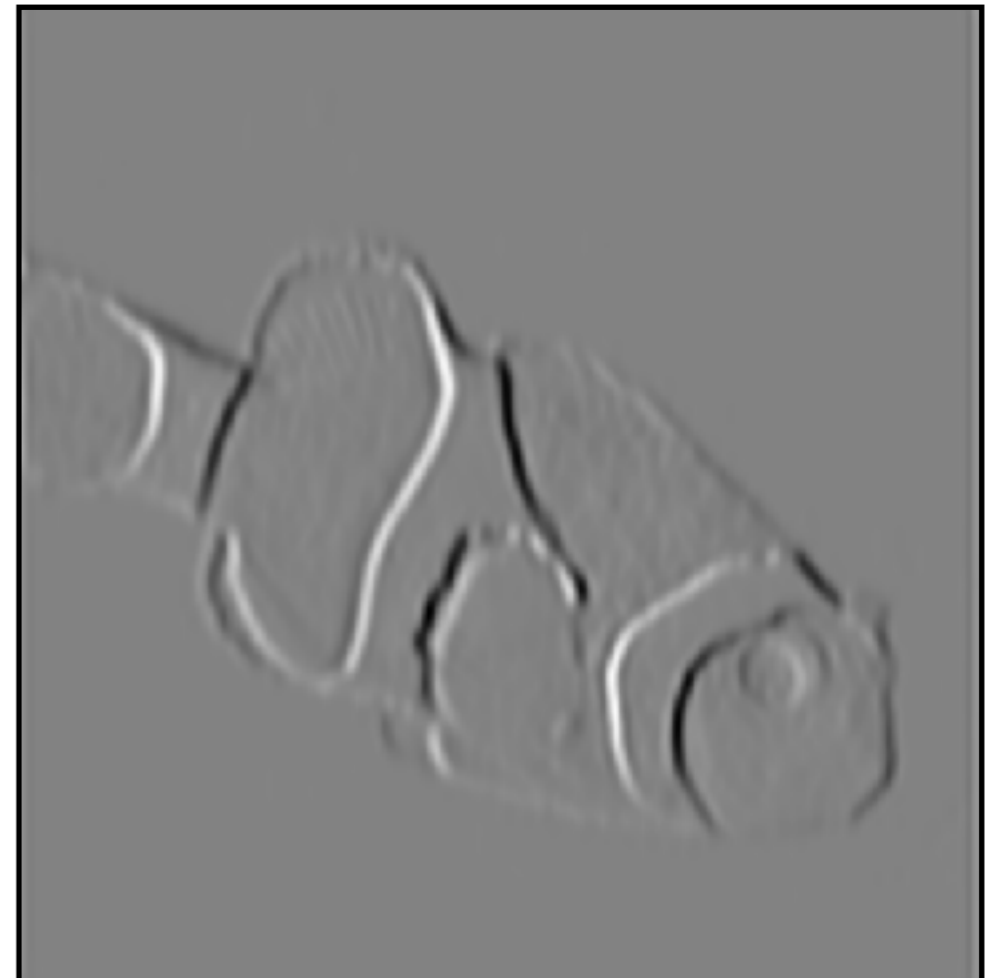
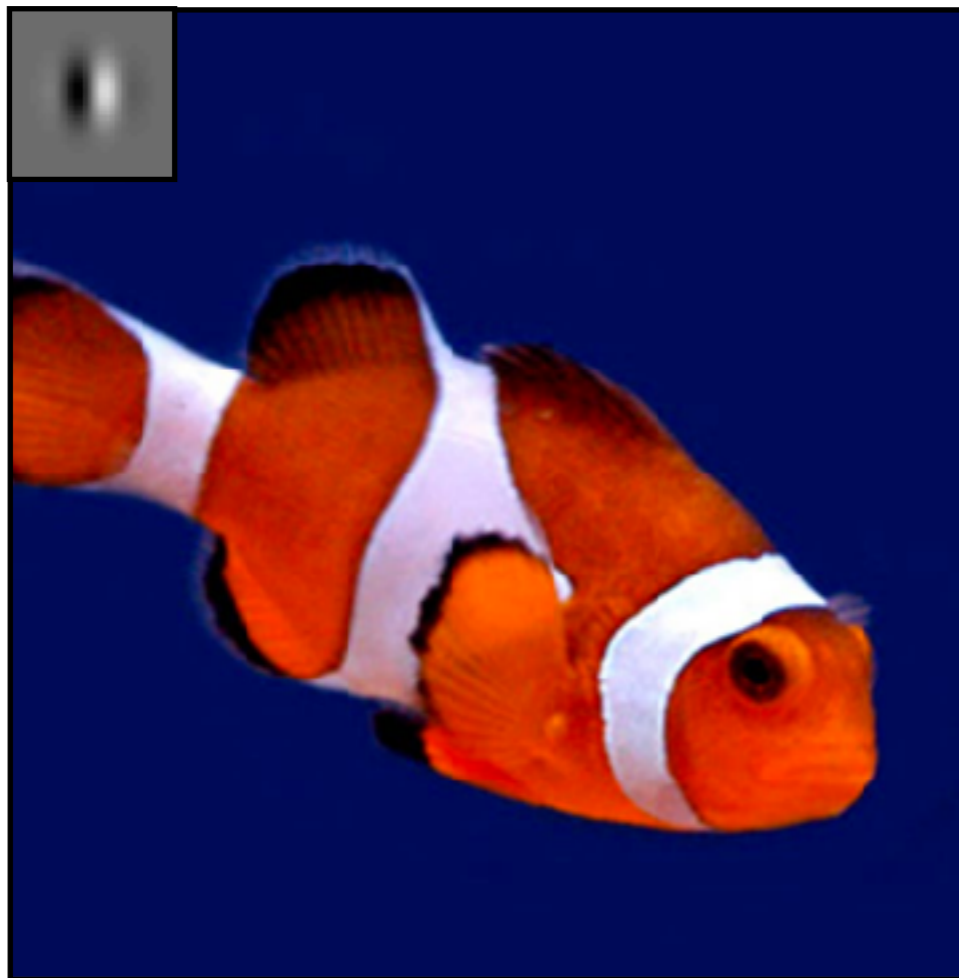
Learning a neural net: learning a simple computer program that maps inputs (raw feature vectors) to outputs (predictions)

Architecting Neural Nets

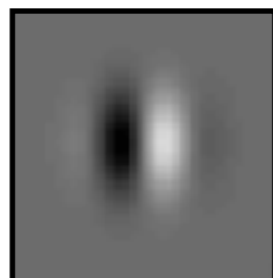
- Increasing number of layers (depth) makes neural net more complex
 - Can approximate more functions
 - More parameters needed
 - More training data may be needed
- Designing neural net architectures is a bit of an art
 - How to select the number of neurons for intermediate layers?
 - Very common in practice: modify existing architectures that are known to work well (e.g., VGG-16 for computer vision/image processing)

**Image analysis with
Convolutional Neural Nets
(CNNs, also called convnets)**

Convolution



filter



Convolution

0	0	0	0	0	0	0
0	0	1	1	1	0	0
0	1	1	1	1	1	0
0	1	1	1	0	0	0
0	1	1	1	1	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0

Input image

0	0	0
0	1	0
0	0	0

Filter
(also called "kernel")

Convolution

0	0	0	0	0	0	0
0	0	1	1	1	0	0
0	1	1	1	1	1	0
0	1	1	1	0	0	0
0	1	1	1	1	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0

Input image

0	0	0
0	1	0
0	0	0

Filter
(also called "kernel")

Convolution

Take dot product!

0	0	0	0	0	0	0
0	0	1	0	1	1	0
0	1	0	1	1	1	0
0	1	1	1	0	0	0
0	1	1	1	1	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0

Input image

0				

Output image

Convolution

Take dot product!

0	0	0	0	0	0	0
0	0	1	1	1	0	0
0	1	1	1	1	1	0
0	1	1	1	0	0	0
0	1	1	1	1	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0

Input image

0	1			

Output image

Convolution

Take dot product!

0	0	0	0	0	0	0
0	0	1	1	1	0	0
0	1	1	0	1	0	1
0	1	1	1	0	0	0
0	1	1	1	1	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0

Input image

0	1	1		

Output image

Convolution

Take dot product!

0	0	0	0	0	0	0
0	0	1	1	1	0	0
0	1	1	1	0	0	0
0	1	1	1	1	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0

Input image

0	1	1	1	

Output image

Convolution

Take dot product!

0	0	0	0	0	0	0
0	0	1	1	1	0	0
0	1	1	1	1	0	0
0	1	1	1	0	0	0
0	1	1	1	1	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0

Input image

0	1	1	1	0

Output image

Convolution

Take dot product!

0	0	0	0	0	0	0		
0	0	0	1	0	1	1	0	0
0	0	1	1	1	0	1	1	0
0	0	1	0	1	0	1	0	0
0	1	1	1	1	1	1	0	
0	0	1	1	1	0	0		
0	0	0	0	0	0	0		

Input image

0	1	1	1	0
1				

Output image

Convolution

Take dot product!

0	0	0	0	0	0	0
0	0	1	0	1	0	1
0	1	0	1	1	0	1
0	1	0	1	0	0	0
0	1	1	1	1	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0

Input image

0	1	1	1	0
1	1			

Output image

Convolution

0	0	0	0	0	0	0
0	0	1	1	1	0	0
0	1	1	1	1	1	0
0	1	1	1	0	0	0
0	1	1	1	1	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0

Input image

*

0	0	0
0	1	0
0	0	0

=

0	1	1	1	0
1	1	1	1	1
1	1	1	0	0
1	1	1	1	1
0	1	1	1	0

Output image

Note: output image is smaller than input image

If you want output size to be same as input, pad 0's to input

Convolution

0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	1	1	1	0	0	0
0	0	1	1	1	1	1	0	0
0	0	1	1	1	0	0	0	0
0	0	1	1	1	1	1	0	0
0	0	0	1	1	1	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0

Input image

*

0	0	0
0	1	0
0	0	0

=

0	0	0	0	0	0	0
0	0	1	1	1	0	0
0	1	1	1	1	1	0
0	1	1	1	0	0	0
0	1	1	1	1	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0

Output image

Note: output image is smaller than input image

If you want output size to be same as input, pad 0's to input

Convolution

0	0	0	0	0	0	0
0	0	1	1	1	0	0
0	1	1	1	1	1	0
0	1	1	1	0	0	0
0	1	1	1	1	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0

Input image

*

0	0	0
0	1	0
0	0	0

=

0	1	1	1	0
1	1	1	1	1
1	1	1	0	0
1	1	1	1	1
0	1	1	1	0

Output image

Convolution

0	0	0	0	0	0	0
0	0	1	1	1	0	0
0	1	1	1	1	1	0
0	1	1	1	0	0	0
0	1	1	1	1	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0

Input image

*	$\frac{1}{9}$	1	1	1
		1	1	1
		1	1	1

=	$\frac{1}{9}$	3	5	6	5	3
		5	8	8	6	3
		6	9	8	7	4
		5	8	8	6	3
		3	5	6	5	3

Output image

Convolution

0	0	0	0	0	0	0
0	0	1	1	1	0	0
0	1	1	1	1	1	0
0	1	1	1	0	0	0
0	1	1	1	1	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0

Input image

*

-1	-1	-1
2	2	2
-1	-1	-1

=

0	1	3	1	0
1	1	1	3	3
0	0	-2	-4	-4
1	1	1	3	3
0	1	3	1	0

Output image

Convolution

Very commonly used for:

- Blurring an image



$$\begin{matrix} * & \begin{matrix} \begin{matrix} 1/9 & 1/9 & 1/9 \\ 1/9 & 1/9 & 1/9 \\ 1/9 & 1/9 & 1/9 \end{matrix} \end{matrix} & = \end{matrix}$$



- Finding edges

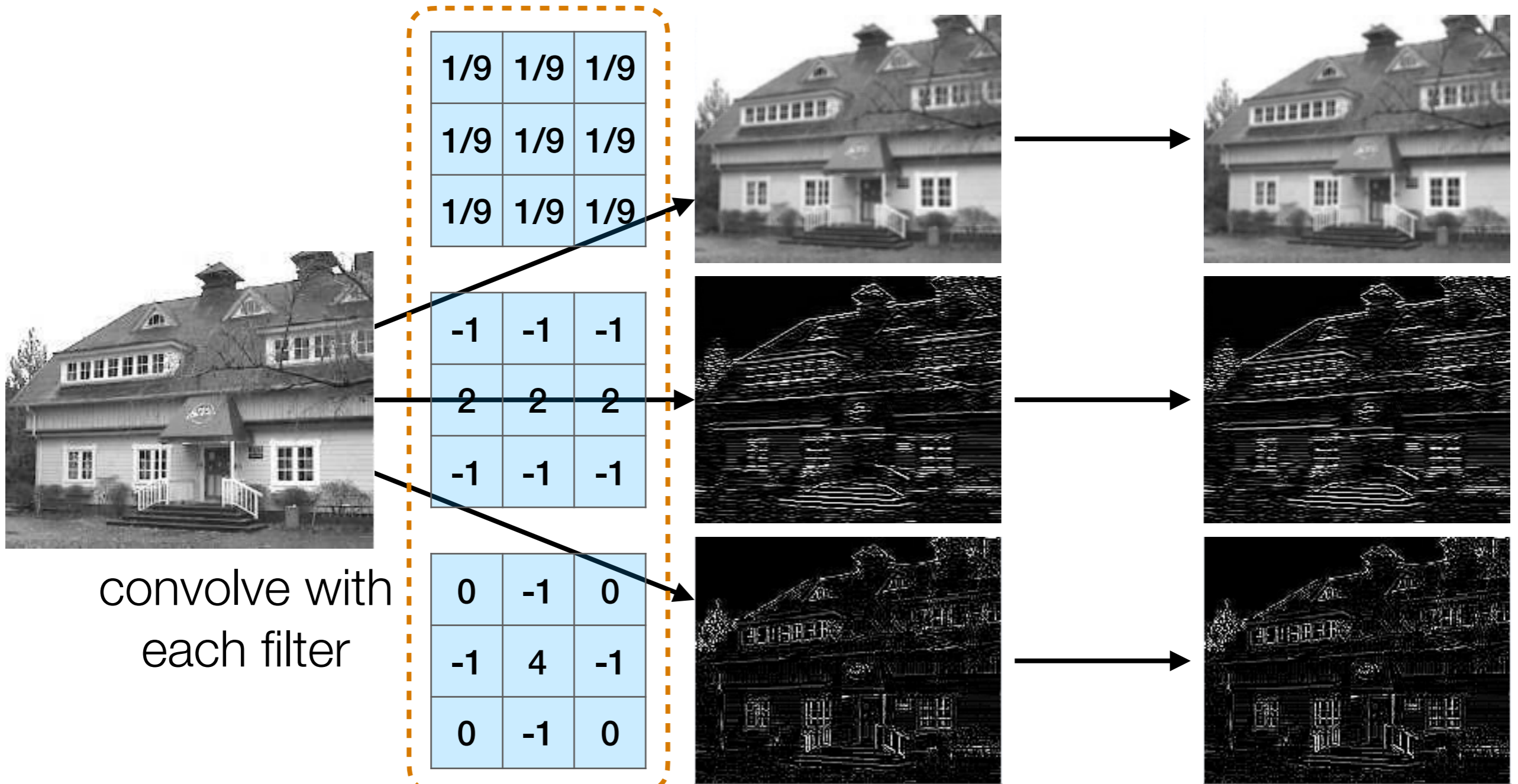


$$\begin{matrix} * & \begin{matrix} \begin{matrix} -1 & -1 & -1 \\ 2 & 2 & 2 \\ -1 & -1 & -1 \end{matrix} \end{matrix} & = \end{matrix}$$



(this example finds horizontal edges)

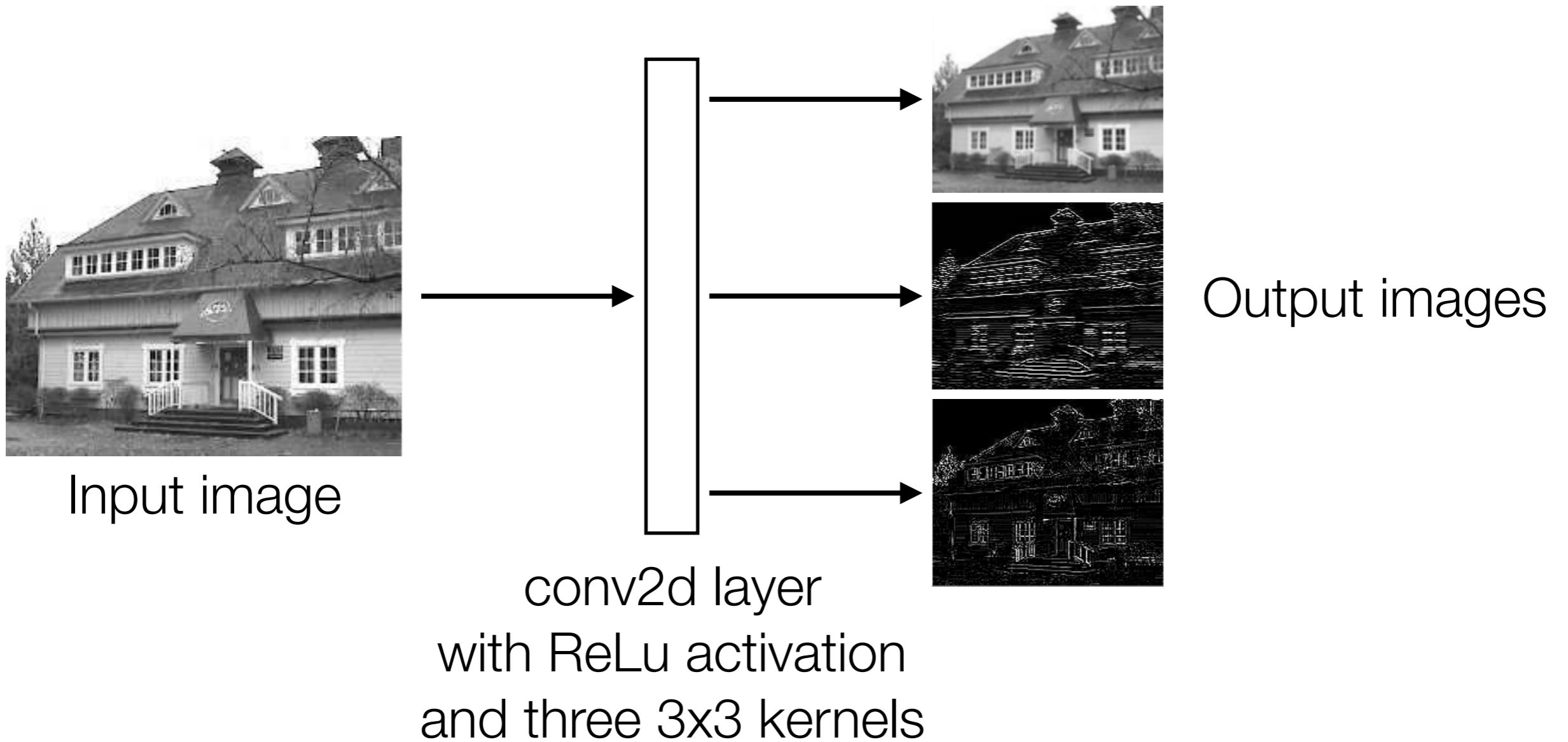
Convolution Layer



filters are actually unknown and are learned!

activation (e.g., ReLU)

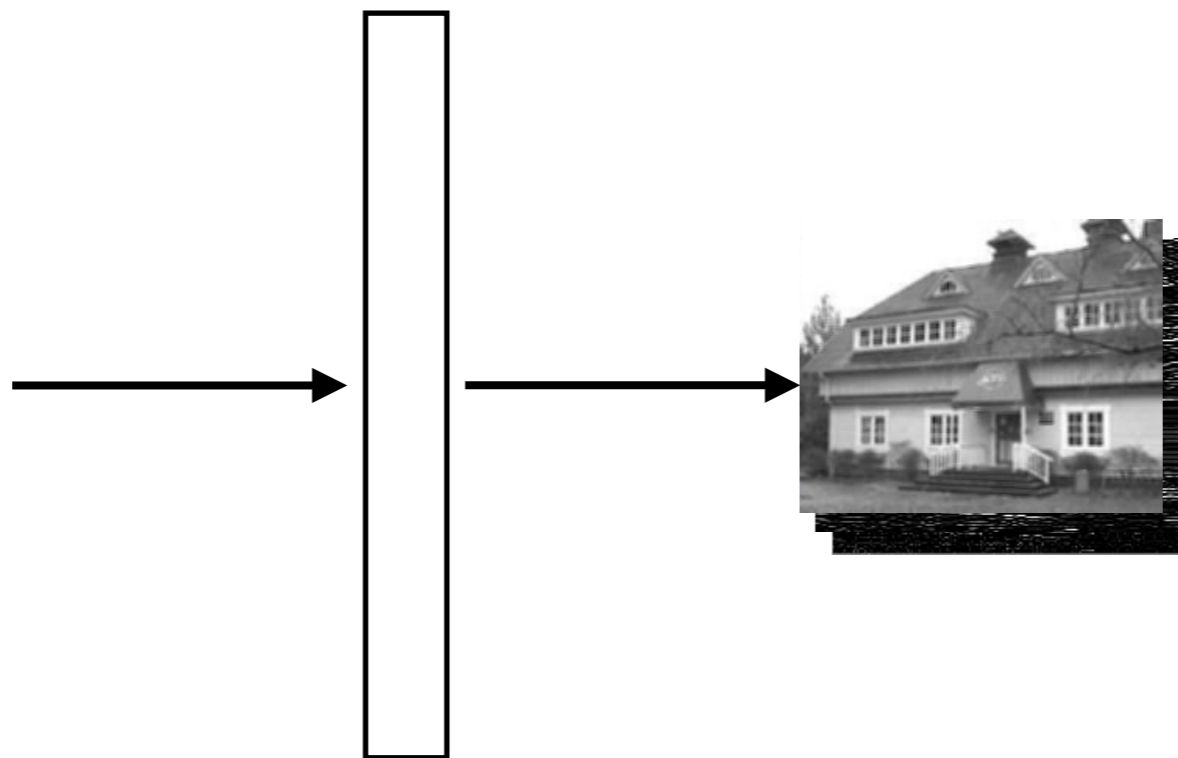
Convolution Layer



Convolution Layer



Input image
dimensions:
height,
width



conv2d layer
with ReLu activation
and three 3x3 kernels

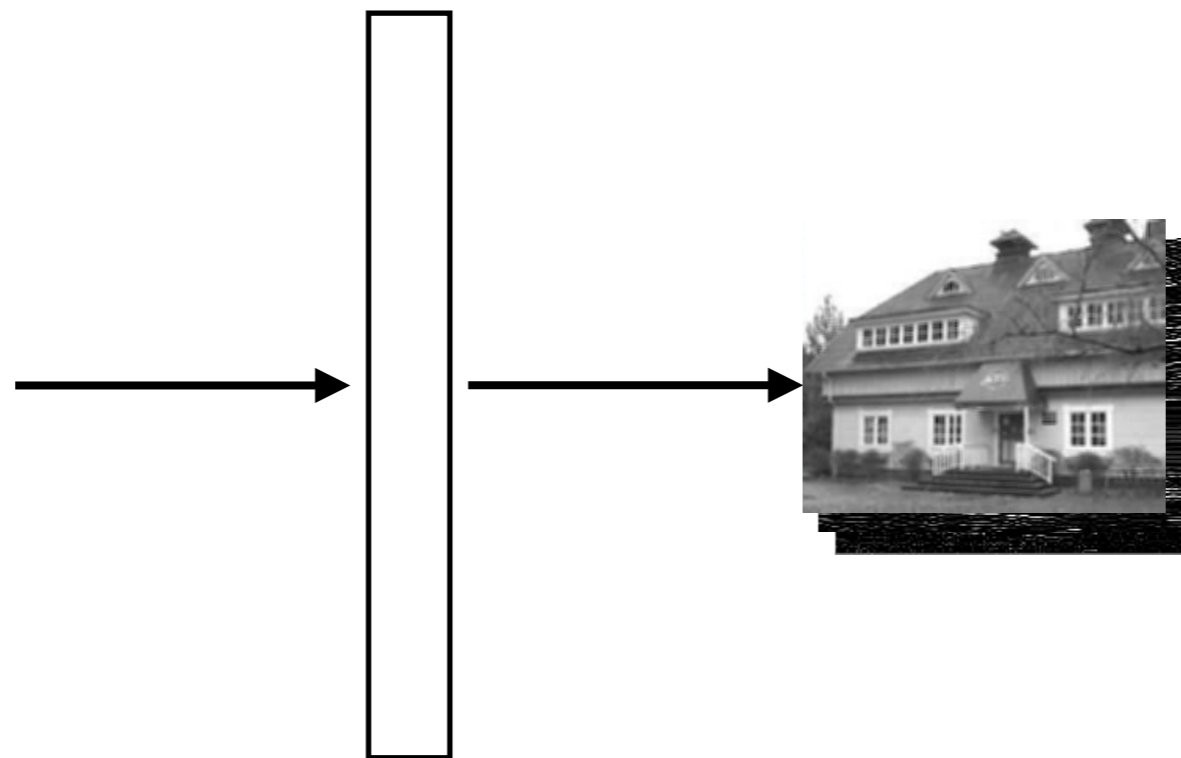


Stack output
images into a
single “output
feature map”
dimensions:
height-2,
width-2,
number of kernels
(3 in this case)

Convolution Layer



Input image
dimensions:
height,
width



conv2d layer
with ReLu activation
and k 3x3 kernels



Stack output
images into a
single “output
feature map”

dimensions:
height-2,
width-2,
 k

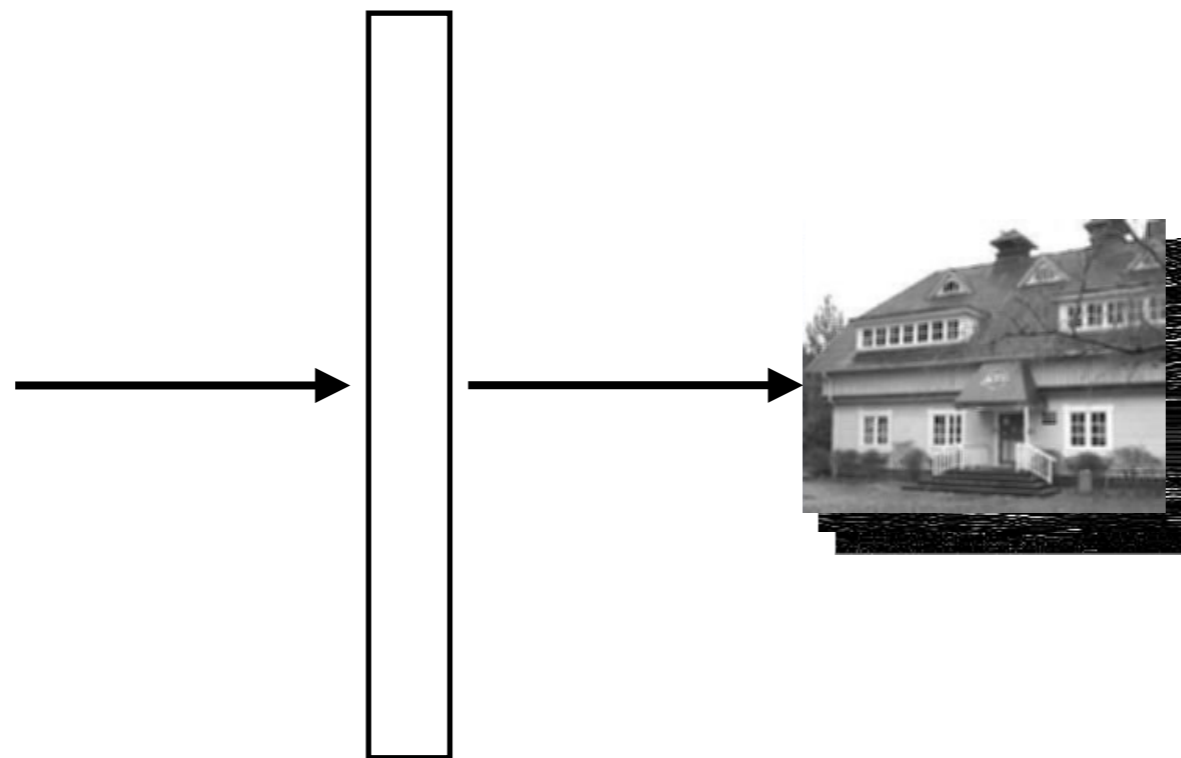
Convolution Layer



Input image

dimensions:
height,
width,

depth d (# channels)



conv2d layer
with ReLu activation
and k $3 \times 3 \times d$ kernels

technical detail: there's
also a bias vector



Stack output
images into a
single “output
feature map”

dimensions:
height-2,
width-2,
 k

Pooling

- Aggregate local information
- Produces a smaller image
(each resulting pixel captures some “global” information)
- If object in input image shifts a little, output is the same

Max Pooling

0	0	0	0	0	0	0
0	0	1	1	1	0	0
0	1	1	1	1	1	0
0	1	1	1	0	0	0
0	1	1	1	1	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0

Input image

$$\begin{array}{|c|c|c|} \hline -1 & -1 & -1 \\ \hline 2 & 2 & 2 \\ \hline -1 & -1 & -1 \\ \hline \end{array} = \begin{array}{|c|c|c|c|c|} \hline 0 & 1 & 3 & 1 & 0 \\ \hline 1 & 1 & 1 & 3 & 3 \\ \hline 0 & 0 & -2 & -4 & -4 \\ \hline 1 & 1 & 1 & 3 & 3 \\ \hline 0 & 1 & 3 & 1 & 0 \\ \hline \end{array}$$

Max Pooling

0	0	0	0	0	0	0
0	0	1	1	1	0	0
0	1	1	1	1	1	0
0	1	1	1	0	0	0
0	1	1	1	1	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0

Input image

-1	-1	-1
2	2	2
-1	-1	-1

*

=

0	1	3	1	0
1	1	1	3	3
0	0	-2	-4	-4
1	1	1	3	3
0	1	3	1	0

0	1	3	1	0
1	1	1	3	3
0	0	0	0	0
1	1	1	3	3
0	1	3	1	0

Output image
after ReLU

Output after
max pooling

Max Pooling

0	0	0	0	0	0	0
0	0	1	1	1	0	0
0	1	1	1	1	1	0
0	1	1	1	0	0	0
0	1	1	1	1	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0

Input image

-1	-1	-1
2	2	2
-1	-1	-1

*

=

0	1	3	1	0
1	1	1	3	3
0	0	-2	-4	-4
1	1	1	3	3
0	1	3	1	0

0	1	3	1	0
1	1	1	3	3
0	0	0	0	0
1	1	1	3	3
0	1	3	1	0

Output image
after ReLU

1	

Output after
max pooling

Max Pooling

0	0	0	0	0	0	0
0	0	1	1	1	0	0
0	1	1	1	1	1	0
0	1	1	1	0	0	0
0	1	1	1	1	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0

Input image

-1	-1	-1
2	2	2
-1	-1	-1

*

=

0	1	3	1	0
1	1	1	3	3
0	0	-2	-4	-4
1	1	1	3	3
0	1	3	1	0

0	1	3	1	0
1	1	1	3	3
0	0	0	0	0
1	1	1	3	3
0	1	3	1	0

Output image
after ReLU

1	3

Output after
max pooling

Max Pooling

0	0	0	0	0	0	0
0	0	1	1	1	0	0
0	1	1	1	1	1	0
0	1	1	1	0	0	0
0	1	1	1	1	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0

Input image

-1	-1	-1
2	2	2
-1	-1	-1

*

=

0	1	3	1	0
1	1	1	3	3
0	0	-2	-4	-4
1	1	1	3	3
0	1	3	1	0

0	1	3	1	0
1	1	1	3	3
0	0	0	0	0
1	1	1	3	3
0	1	3	1	0

Output image
after ReLU

1	3
1	

Output after
max pooling

Max Pooling

0	0	0	0	0	0	0
0	0	1	1	1	0	0
0	1	1	1	1	1	0
0	1	1	1	0	0	0
0	1	1	1	1	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0

Input image

-1	-1	-1
2	2	2
-1	-1	-1

*

=

0	1	3	1	0
1	1	1	3	3
0	0	-2	-4	-4
1	1	1	3	3
0	1	3	1	0

0	1	3	1	0
1	1	1	3	3
0	0	0	0	0
1	1	1	3	3
0	1	3	1	0

Output image
after ReLU

1	3
1	3

Output after
max pooling

Max Pooling

0	0	0	0	0	0	0
0	0	1	1	1	0	0
0	1	1	1	1	1	0
0	1	1	1	0	0	0
0	1	1	1	1	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0

Input image

-1	-1	-1
2	2	2
-1	-1	-1

*

=

0	1	3	1	0
1	1	1	3	3
0	0	-2	-4	-4
1	1	1	3	3
0	1	3	1	0

0	1	3	1	0
1	1	1	3	3
0	0	0	0	0
1	1	1	3	3
0	1	3	1	0

Output image after ReLU

What numbers were involved in computing this 1?

In this example: 1 pixel in max pooling output captures information from 16 input pixels!

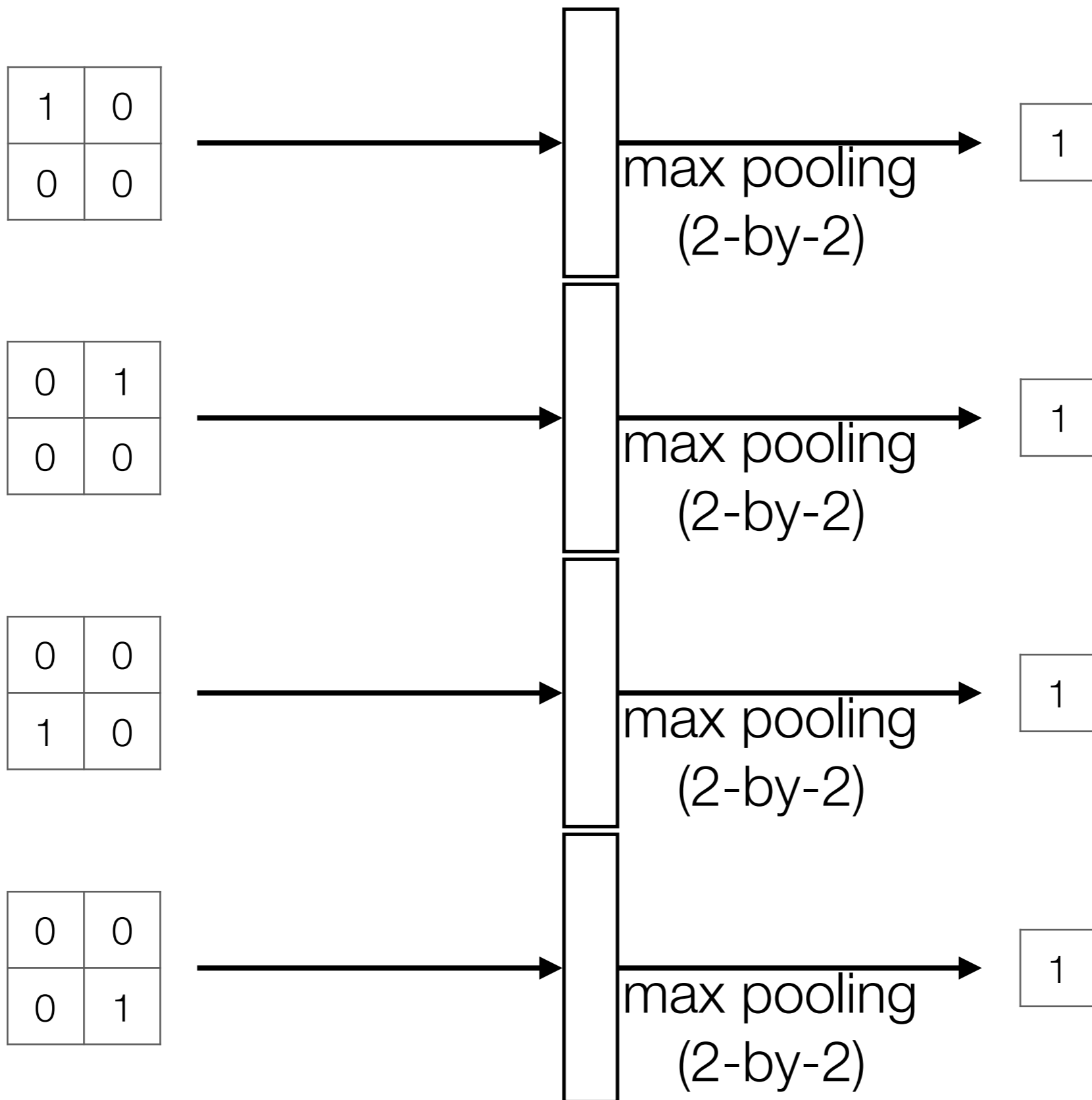
Example: applying max pooling again results in a single pixel that captures info from entire input image!

1	3
1	3

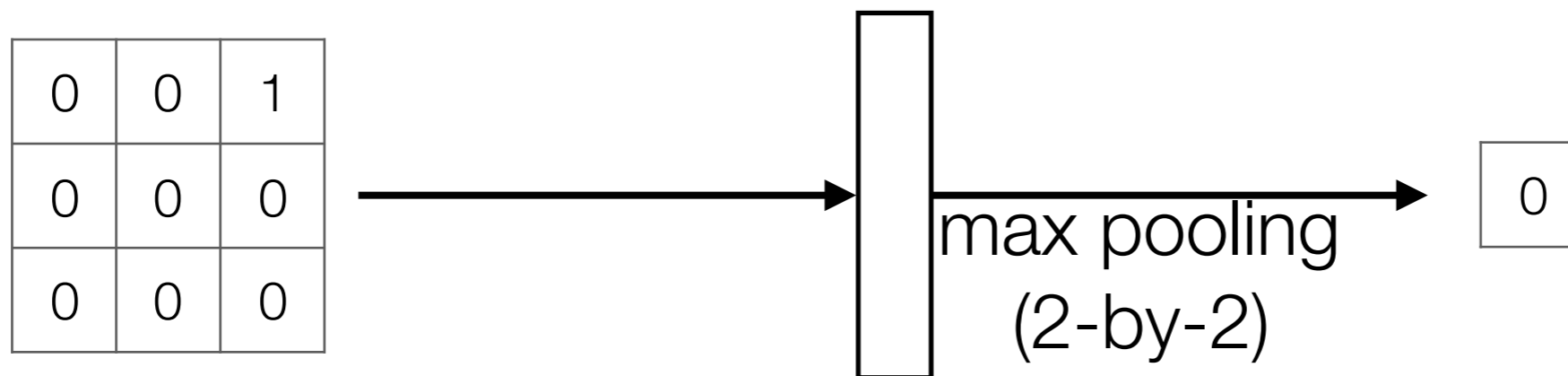
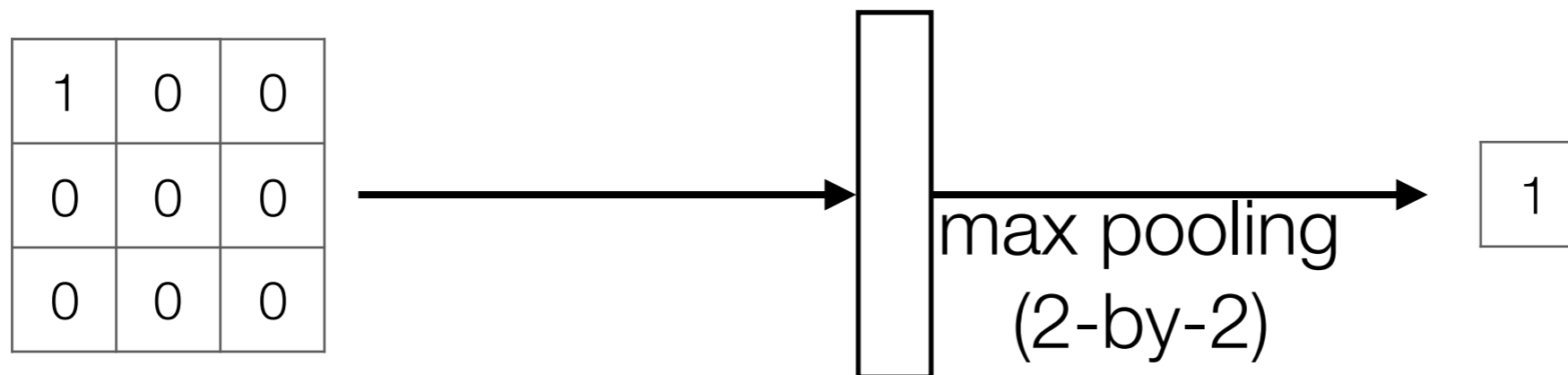
Output after max pooling

Max Pooling and (Slight) Shift Invariance

Small shift
of object in
input
image
results in
same
output

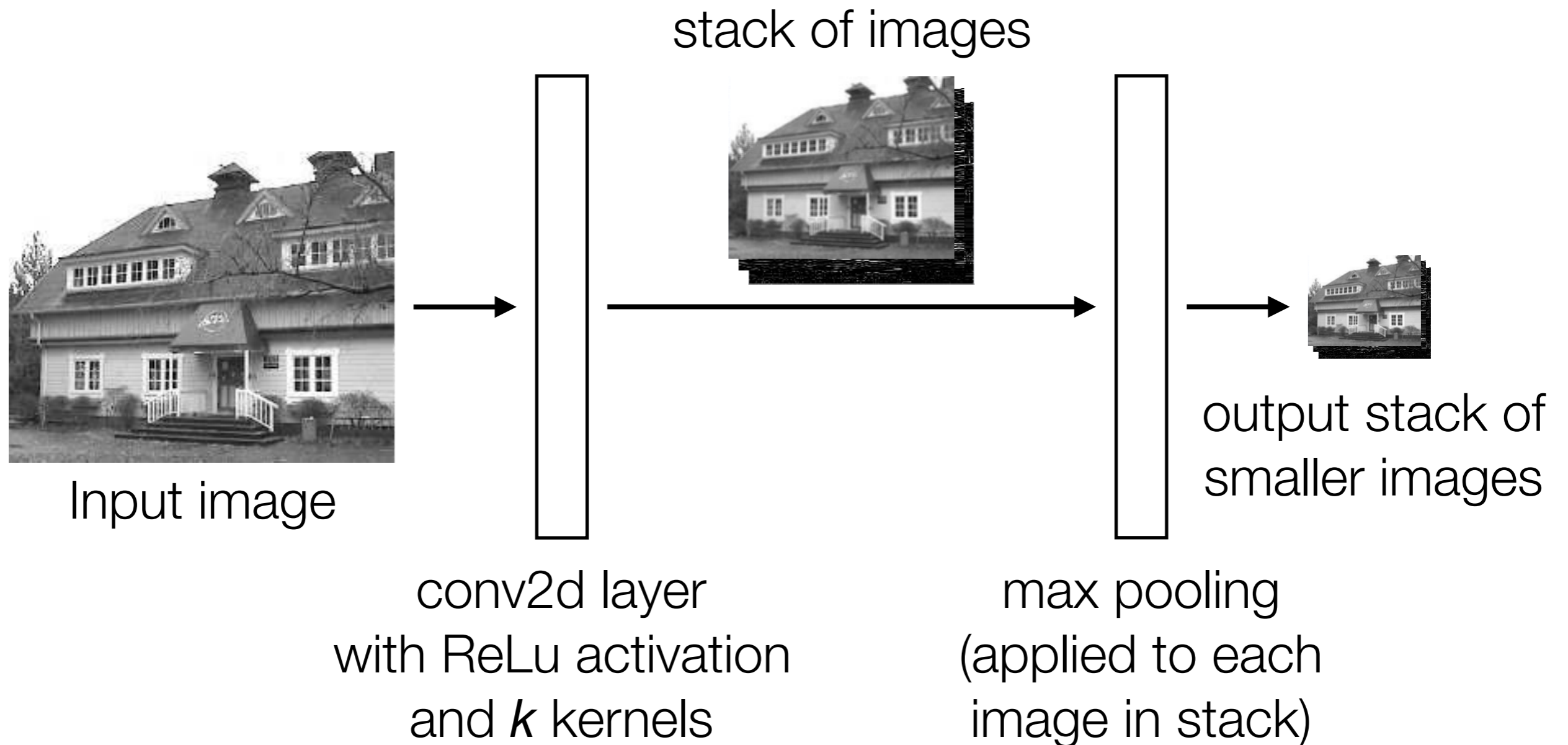


Max Pooling and (Slight) Shift Invariance



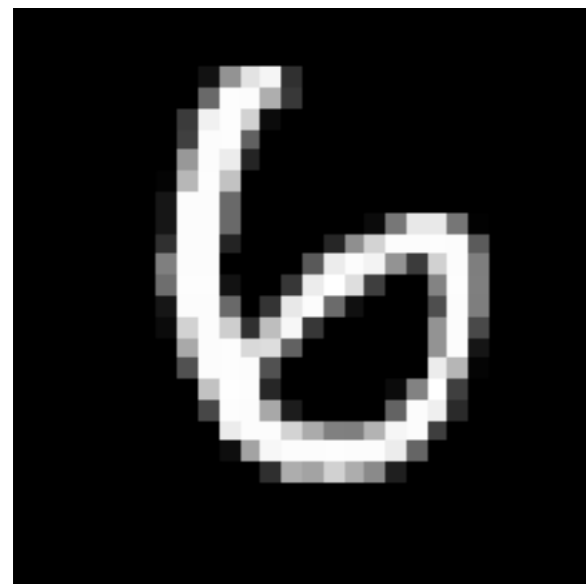
Big shift in input can still change output

Basic Building Block of CNN's



Handwritten Digit Recognition

Training label: 6



28x28 image

length 784 vector
(784 input neurons)

Learning this neural net means learning parameters of both dense layers!



dense layer with 512 neurons, ReLU activation

dense layer with 10 neurons, softmax activation

Loss/"error"

Popular loss function for classification (> 2 classes): **categorical cross entropy**

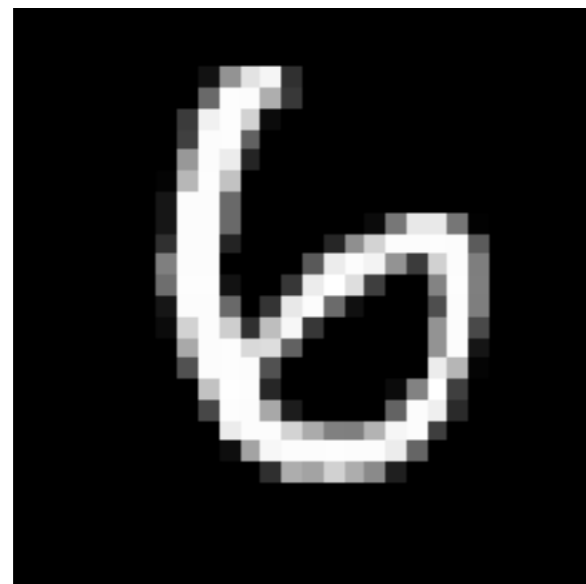
$$\log \frac{1}{\text{Pr}(\text{digit } 6)}$$

Error is averaged across training examples

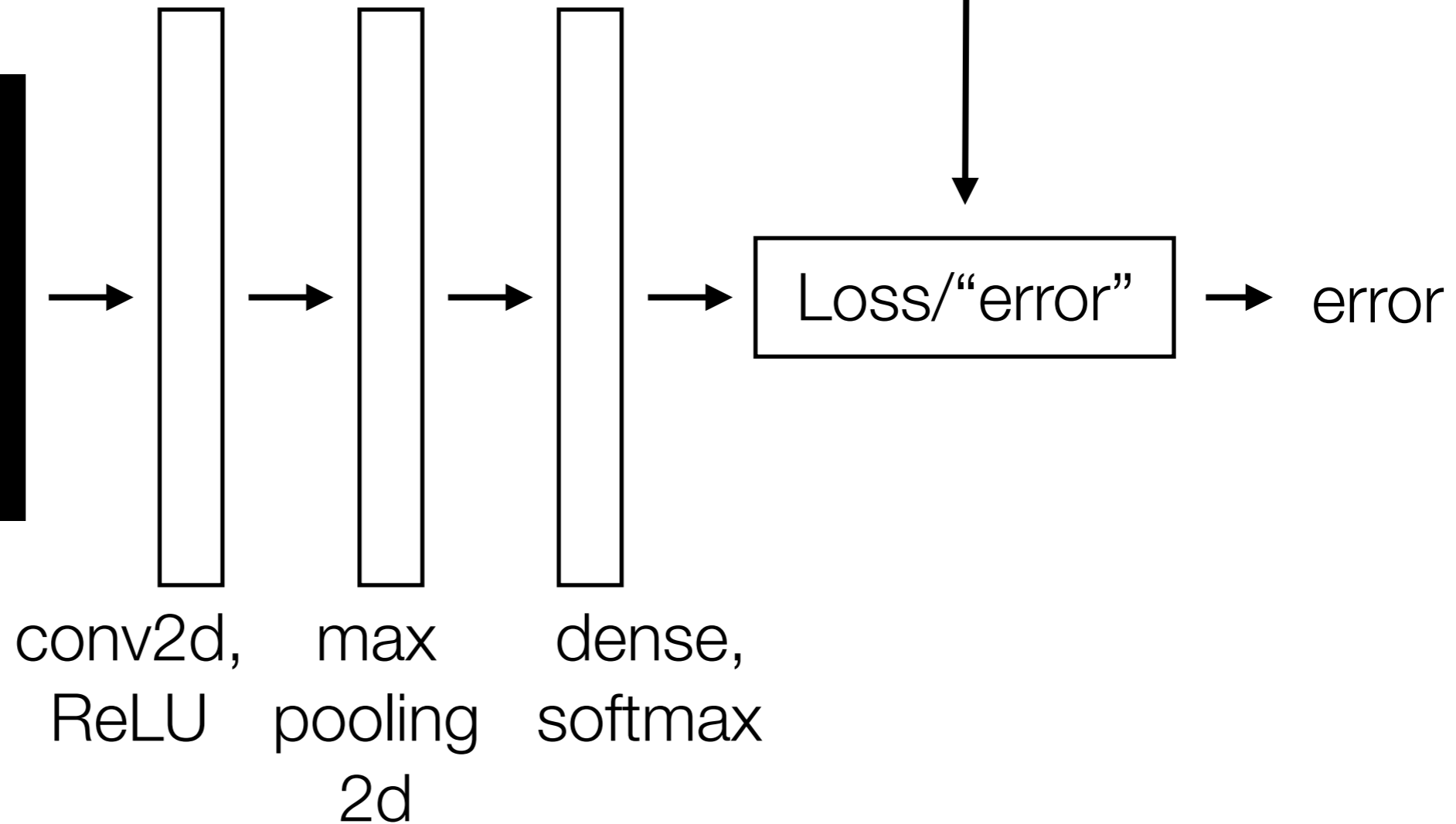
error

Handwritten Digit Recognition

Training label: 6

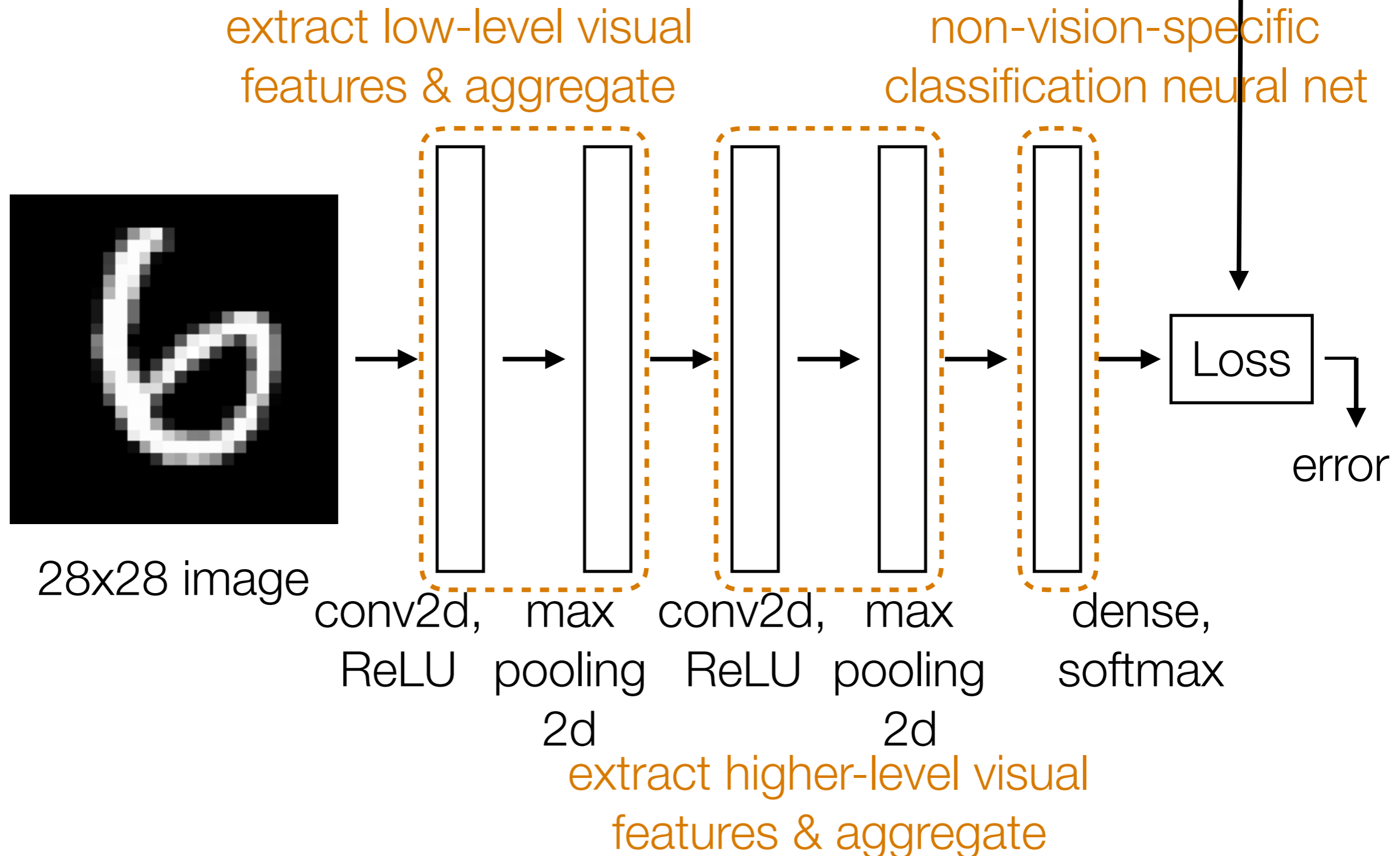


28x28 image



Handwritten Digit Recognition

Training label: 6



CNN Demo

CNN's

- Learn convolution filters for extracting simple features
- Max pooling summarizes information and produces a *smaller* output and is invariant to small shifts in input objects
- Can then repeat the above two layers to learn features from increasingly higher-level representations